

extra credit: Ch 12 problem 32

atmospheric pressure = $1.013 \times 10^5 \text{ N/m}^2$

a) with $\Delta P = 1.13 \times 10^8 \text{ N/m}^2 - 1.013 \times 10^5 \text{ N/m}^2 \approx 1.13 \times 10^8 \text{ N/m}^2$,

change in volume from $B = -\frac{\Delta P}{\Delta V/V_L} = -\frac{\Delta P V_L}{\Delta V}$

$$\Rightarrow \Delta V = -\frac{\Delta P V_L}{B}$$

for water with $V_L = 1.00 \text{ m}^3$, $B = 0.21 \times 10^{10} \text{ N/m}^2$

$$\Delta V = -\frac{(1.13 \times 10^8 \text{ N/m}^2)(1 \text{ m}^3)}{0.21 \times 10^{10} \text{ N/m}^2} = -0.0538 \text{ m}^3$$

that is, decreases in volume by 0.0538 m^3

new volume = 0.95 m^3

b) density at surface $\rho = m/V = 1.03 \times 10^3 \text{ kg/m}^3$

so 1.00 m^3 of seawater has $m = 1.03 \times 10^3 \text{ kg}$

at 11 km deep, $\rho = \frac{1.03 \times 10^3 \text{ kg}}{0.95 \text{ m}^3} = 1.09 \times 10^3 \text{ kg/m}^3$

c) since the volume + density change by only about 5% even under these extreme conditions, it's usually a good approximation to think of water as incompressible